



TIME: 2:30

M.M. 300

**CENTURION DEFENCE ACADEMY
NDA MODAL TEST PAPER – MATHEMATICS**

INSTRUCTION: Read questions carefully. For each wrong answer, one-third (0.833) of the marks assigned to that question will be deducted. Each question contains (2.5) marks. / प्रश्नों को ध्यानपूर्वक पढ़िए। प्रत्येक गलत उत्तर के लिए, $\frac{1}{3}$ अंक काटे जायेंगे। प्रत्येक प्रश्न (2.5) अंक का है।

- Consider the following statements in respect of a histogram:
 - The total area of the rectangles in a histogram is equal to the total area bounded by the corresponding frequency polygon and the x -axis.
 - When class intervals are unequal in a frequency distribution, the area of the rectangle is proportional to the frequency.
 Which of the above statements is/are correct?

(A) 1 only	(B) 2 only
(C) Both 1 and 2	(D) Neither 1 nor 2
- Consider a parallelogram whose vertices are $A(1, 2), B(4, y), C(x, 6)$ and $D(3, 5)$ taken in order. What is the point of intersection of the diagonals?

(A) $(\frac{7}{2}, 4)$	(B) $(3, 4)$
(C) $(\frac{7}{2}, 5)$	(D) $(3, 5)$
- Consider the function $f(x) = |x^2 - 5x + 6|$. What is $f'(4)$ equal to?

(A) -4	(B) -3
(C) 3	(D) 2
- What is the probability of 5 Sundays in the month of December?

(A) $\frac{1}{7}$	(B) $\frac{2}{7}$
(C) $\frac{3}{7}$	(D) None of the above
- If two dice are thrown, then what is the probability that the sum on the two faces is greater than or equal to 4?

(A) $\frac{13}{18}$	(B) $\frac{5}{6}$
(C) $\frac{11}{12}$	(D) $\frac{35}{36}$
- Let $f: R \rightarrow R$ be a function such that $f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3)$ for $x \in R$. What is $f(1)$ equal to?

(A) -2	(B) -1
(C) 0	(D) 4
- Consider the equation $k \sin x + \cos 2x = 2k - 7$. If the equation possesses solution, then what is the maximum value of k ?

(A) 1	(B) 2
(C) 4	(D) 6

8. Let z be a complex number satisfying $\left|\frac{z-4}{z-8}\right| = 1$ and $\left|\frac{z}{z-2}\right| = \frac{3}{2}$.
 $\left|\frac{z}{z-2}\right| = \frac{3}{2}$ को संतुष्ट करती है।
 What is $\left|\frac{z-6}{z-6}\right|$ equal to?
 (A) 3 (B) 2
 (C) 1 (D) 0
9. Consider the two lines $x + y + 1 = 0$ and $3x + 2y + 1 = 0$.
 What is the equation of the line passing through the point of intersection of the given lines and parallel to y -axis?
 (A) $x + 1 = 0$ (B) $x - 1 = 0$
 (C) $x - 2 = 0$ (D) $x + 2 = 0$
10. A plane P passes through the line of intersection of the planes $2x - y + 3z = 2$, $x + y - z = 1$ and the point $(1, 0, 1)$.
 If the plane P touches the sphere $x^2 + y^2 + z^2 = r^2$, then what is r equal to?
 (A) $\frac{2}{\sqrt{29}}$ (B) $\frac{4}{\sqrt{29}}$
 (C) $\frac{5}{\sqrt{29}}$ (D) 1
11. What is the number of four-digit decimal numbers (< 1) in which no digit is repeated?
 (A) 3024 (B) 4536
 (C) 5040 (D) None of the above
12. Suppose ω_1 and ω_2 are two distinct cube roots of unity different from 1. Then what is $(\omega_1 - \omega_2)^2$ equal to?
 (A) 3 (B) 1
 (C) -1 (D) -3
13. A plane P passes through the line of intersection of the planes $2x - y + 3z = 2$, $x + y - z = 1$ and the point $(1, 0, 1)$.
 What is the equation of the plane P ?
 (A) $2x + 5y - 2 = 0$ (B) $5x + 2y - 5 = 0$
 (C) $x + z - 2 = 0$ (D) $2x - y - 2z = 0$
14. What is the area of the parallelogram having diagonal $3\hat{i} + \hat{j} - 2\hat{k}$ and $\hat{i} - 3\hat{j} + 4\hat{k}$?
 (A) $5\sqrt{5}$ square units (B) $4\sqrt{5}$ square units
 (C) $5\sqrt{3}$ square units (D) $15\sqrt{2}$ square units
15. Let z_1, z_2 and z_3 be non-zero complex numbers satisfying $z^2 = i\bar{z}$, where $i = \sqrt{-1}$.
 Consider the following statements:
 1. $z_1 z_2 z_3$ is purely imaginary.
 2. $z_1 z_2 + z_2 z_3 + z_3 z_1$ is purely real.
 Which of the above statements is/ are correct?
 (A) 1 only (B) 2 Only
 (C) Both 1 and 2 (D) Neither 1 nor 2
16. Consider the function $f(x) = \frac{a^{|x|+x}-1}{|x|+x}$ where $[.]$ denotes the greatest integer function.
 What is $\lim_{x \rightarrow 0^-} f(x)$ equal to?
 (A) 1 (B) $\ln a$
 (C) $1 - a^{-1}$ (D) Limit does not exist

17. What is a vector of unit length orthogonal to both the vectors $\hat{i} + \hat{j} + \hat{k}$ and $2\hat{i} + 3\hat{j} - \hat{k}$? / दो सदिशों $\hat{i} + \hat{j} + \hat{k}$ व $2\hat{i} + 3\hat{j} - \hat{k}$ के लंबकोणिक एकक लंबाई का सदिश क्या है\
- (A) $\frac{-4\hat{i} + 3\hat{j} - \hat{k}}{\sqrt{26}}$ (B) $\frac{-4\hat{i} + 3\hat{j} + \hat{k}}{\sqrt{26}}$
 (C) $\frac{-3\hat{i} + 2\hat{j} - \hat{k}}{\sqrt{14}}$ (D) $\frac{-3\hat{i} + 2\hat{j} + \hat{k}}{\sqrt{14}}$
18. Let α and β ($\alpha < \beta$) be the roots of the equation $x^2 + bx + c = 0$, where $b > 0$ and $c > 0$. / eku yhf, fd α व β ($\alpha < \beta$) l ehj. k $x^2 + bx + c = 0$ ds ey gñ tgk $b > 0$ व $c > 0$ gñ
 Consider the following: / fuEufyf[kr ij fopkj dhft, %
 1. $\beta < -\alpha$
 2. $\beta < |\alpha|$
 Which of the above is/are correct? / mi ; Dr dFkuk eñ l s dku&l k@l s l gh gñgñ
 (A) 1 Only / dpy 1 (B) 2 Only / dpy 2
 (C) both 1 and 2 / 1 व 2 nkuka (D) Neither 1 nor 2 / u rks 1 व 2 u gh 2
19. Consider the following in respect of the matrix $A = \begin{pmatrix} -1 & 1 \\ 1 & -1 \end{pmatrix}$: / vk; g $A = \begin{pmatrix} -1 & 1 \\ 1 & -1 \end{pmatrix}$ ds ckjs eñ fuEufyf[kr ij fopkj dhft, %
 1. $A^2 = -A$
 2. $A^3 = 4A$
 Which of the above is/are correct? / mi ; Dr eñ l s dku&l k@l s l gh gñgñ
 (A) 1 only / dpy 1 (B) 2 only / dpy 2
 (C) Both 1 and 2 / 1 व 2 nkuka (D) Neither 1 nor 2 / u rks 1 व 2 u gh 2
20. Consider a parallelogram whose vertices are $A(1, 2), B(4, y), C(x, 6)$ and $D(3, 5)$ taken in order. /, d l ekj pñkñt] जिसके शीर्ष, एक क्रम में, $A(1, 2), B(4, y), C(x, 6)$ व $D(3, 5)$ gñ ij fopkj dhft, A
 What is the area of the parallelogram? / l ekj pñkñt dk {k=Qy D; k gñ
 (A) $\frac{7}{2}$ square units / $\frac{7}{2}$ oxl bdkbz (B) 4 square units / 4 oxl bdkbz
 (C) $\frac{11}{2}$ square units / $\frac{11}{2}$ oxl bdkbz (D) 7 square units / 7 oxl bdkbz
21. Given that $\tan \alpha$ and $\tan \beta$ are the roots of the equation $x^2 + bx + c = 0$ with $b \neq 0$. /fn; k x; k gñ fd $\tan \alpha$ व $\tan \beta$ l ehj. k $x^2 + bx + c = 0$ ds ey gñ tgk $b \neq 0$ gñ
 What is $\sin(\alpha + \beta) \sec \alpha \sec \beta$ equal to? / $\sin(\alpha + \beta) \sec \alpha \sec \beta$ fdl ds ckj gñ
 (A) b (B) -b
 (C) c (D) -c
22. Given that $\tan \alpha$ and $\tan \beta$ are the roots of the equation $x^2 + bx + c = 0$ with $b \neq 0$. /fn; k x; k gñ fd $\tan \alpha$ व $\tan \beta$ l ehj. k $x^2 + bx + c = 0$ ds ey gñ tgk $b \neq 0$ gñ
 What is $\tan(\alpha + \beta)$ equal to? / $\tan(\alpha + \beta)$ fdl ds ckj gñ
 (A) $b(c - 1)$ (B) $c(b - 1)$
 (C) $c(b - 1)^{-1}$ (D) $b(c - 1)^{-1}$
23. Consider the two circles $(x - 1)^2 + (y - 3)^2 = r^2$ and $x^2 + y^2 - 8x + 2y + 8 = 0$ /nks oRrk $(x - 1)^2 + (y - 3)^2 = r^2$ व $x^2 + y^2 - 8x + 2y + 8 = 0$ ij fopkj dhft, A
 What is the distance between the centres of the two circles? /nkuk oRrk ds dñæk ds chp dh njh D; k gñ
 (A) 5 units / 5 bdkbz (B) 6 units / 6 bdkbz
 (C) 8 units / 8 bdkbz (D) 10 units / 10 bdkbz
24. Let $f: R \rightarrow R$ be a function such that $f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3)$ for $x \in R$. /eku yhf, fd , d Qy $f: R \rightarrow R$ bl çdkj gñ fd $x \in R$ ds fy, $f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3)$ gñ
 What is $f'''(10)$ equal to? / $f'''(10)$ fdl ds ckj gñ
 (A) 1 (B) 5
 (C) 6 (D) 8
25. Consider a triangle ABC in which $\cos A + \cos B + \cos C = \sqrt{3} \sin \frac{\pi}{3}$ /, d f=Hkñt ABC ft l eñ $\cos A + \cos B + \cos C = \sqrt{3} \sin \frac{\pi}{3}$ gñ ij fopkj dhft, A
 What is the value of $\cos \left(\frac{A+B}{2}\right) \cos \left(\frac{B+C}{2}\right) \cos \left(\frac{C+A}{2}\right)$? / $\cos \left(\frac{A+B}{2}\right) \cos \left(\frac{B+C}{2}\right) \cos \left(\frac{C+A}{2}\right)$ dk eku D; k gñ
 (A) $\frac{1}{4}$ (B) $\frac{1}{2}$
 (C) $\frac{1}{16}$ (D) None of the above / mi ; Dr eñ l s dkbz ugha

26. If \vec{a} , \vec{b} and \vec{c} are the position vectors of the vertices of an equilateral triangle whose orthocenter is at the origin, then which one of the following is correct? /; fn \vec{a} , \vec{b} vkj \vec{c} l eckgf =Hkqt d] जिसका लंबकेन्द्र मूलबिंदू पर है, शीर्षों के स्थिति सदिश हैं, तो निम्नलिखित में से कौन सा एक सही है\

- (A) $\vec{a} + \vec{b} + \vec{c} = 0$ (B) $\vec{a} + \vec{b} + \vec{c} = \text{unit vector}$ /एकक सदिश
(C) $\vec{a} + \vec{b} = \vec{c}$ (D) $\vec{a} = \vec{b} + \vec{c}$

27. Consider the two lines $x + y + 1 = 0$ and $3x + 2y + 1 = 0$ /nks js[$kkvka$ $x + y + 1 = 0$ vkj $3x + 2y + 1 = 0$ ij fopkj dhft, A

What is the equation of the line passing through the point of intersection of the given lines and parallel to x -axis? /nh xbl js[$kkvka$ ds cfrPNn fcaq l s xqtjus okyh vkj x -v{k ds l ekarj js[kk dk l ehjdj .k D; k g\

- (A) $y + 1 = 0$ (B) $y - 1 = 0$
(C) $y - 2 = 0$ (D) $y + 2 = 0$

28. A function $f(x)$ is defined as follows: /, d Qyu $f(x)$ के रूप में परिभाषित है:

$$f(x) = \begin{cases} x + \pi & \text{for } x \in [-\pi, 0) \\ \pi \cos x & \text{for } x \in [0, \frac{\pi}{2}] \\ (x - \frac{\pi}{2})^2 & \text{for } x \in (\frac{\pi}{2}, \pi] \end{cases}$$

Consider the following statements: /fuEufyf[kr dFkuk ij fopkj dhft, %

1. The function $f(x)$ is differentiable at $x = 0$. / Qyu $f(x)$, $x = 0$ ij vodyuh; g\

2. The function $f(x)$ is differentiable at $x = \frac{\pi}{2}$. / Qyu $f(x)$, $x = \frac{\pi}{2}$ ij vodyuh; g\

Which of the above statements is/are correct? / mi ; Dr dFkuka ea l s dkU&l k@l s l gh g@g\

- (A) 1 Only /doy 1 (B) 2 Only /doy 2
(C) both 1 and 2 / vkj 2 nkuka (D) Neither 1 nor 2 /u rks 1 vkj u gh 2

29. A function $f(x)$ is defined as follows: /, d Qyu $f(x)$ के रूप में परिभाषित है:

$$f(x) = \begin{cases} x + \pi & \text{for } x \in [-\pi, 0) \\ \pi \cos x & \text{for } x \in [0, \frac{\pi}{2}] \\ (x - \frac{\pi}{2})^2 & \text{for } x \in (\frac{\pi}{2}, \pi] \end{cases}$$

Consider the following statements: /fuEufyf[kr dFkuk ij fopkj dhft, %

1. The function $f(x)$ is continuous at $x = 0$. /Qyu $f(x)$, $x = 0$ ij l rr g\

2. The function $f(x)$ is continuous at $x = \frac{\pi}{2}$. / Qyu $f(x)$, $x = \frac{\pi}{2}$ ij l rr g\

Which of the above statements is/are correct? /mi ; Dr dFkuka ea l s dkU&l k@l s l gh g@g\

- (A) 1 Only /doy 1 (B) 2 Only /doy 2
(C) both 1 and 2 / vkj 2 nkuka (D) Neither 1 nor 2 /u rks 1 vkj u gh 2

30. Given that $\log_x y$, $\log_z x$, $\log_y z$ are in GP, $xyz = 64$ and x^3, y^3, z^3 are in AP. /fn; k x; k gsf d $\log_x y$, $\log_z x$, $\log_y z$ GP ea g\ $xyz = 64$ g\ vkj x^3, y^3, z^3 ea AP g\

Which one of the following is correct? /fuEufyf[kr ea l s dkU&l k , d l gh g\ x, y and $z/x, y$ vkj z

- (A) in AP Only /doy AP ea g\ (B) In GP Only / doy GP ea g\
(C) In both AP and GP / AP rFk GP nkuka ea g\ (D) neither in AP nor in GP /u rks AP ea vkj u gh GP ea g\

31. Consider the two circles $(x - 1)^2 + (y - 3)^2 = r^2$ and $x^2 + y^2 - 8x + 2y + 8 = 0$ /nks oRrk $(x - 1)^2 + (y - 3)^2 = r^2$ vkj $x^2 + y^2 - 8x + 2y + 8 = 0$ ij fopkj dhft, A

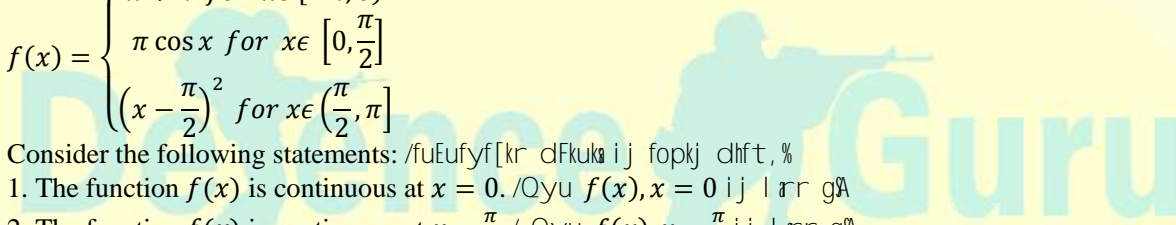
If the circles intersect at two distinct points, then which one of the following is correct? /; fn oRr nks vvx&vyx fcnvka ij cfrPNn djrs g\ rks fuEufyf[kr ea dkU&l k , d l gh g\

- (A) $r = 1$ (B) $1 < r < 2$
(C) $r = 2$ (D) $2 < r < 8$

32. A fair coin is tossed 100 times. What is the probability of getting tails an odd number of times? /, d U; k; fl Ddk 100 ckj mNkyk जाता है। उतनी बार, जो कि एक विषम संख्या हो, तो पट आने की प्रायिकता क्या है\

- (A) $\frac{1}{2}$ (B) $\frac{3}{8}$
(C) $\frac{1}{4}$ (D) $\frac{1}{8}$

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33. The system of linear equations $kx + y + z = 1$, $x + ky + z = 1$ and $x + y + kz = 1$ has a unique solution under which one of the following conditions? / jf [kd l ehdj .k fudk; $kx + y + z = 1$, $x + ky + z = 1$ vkj $x + y + kz = 1$ dk , dek= gy gkxk] ; fn
- (A) $k \neq 1$ and $k \neq -2$ / $k \neq 1$ vkj $k \neq -2$ (B) $k \neq 1$ and $k \neq 2$ / $k \neq 1$ vkj $k \neq 2$
(C) $k \neq -1$ and $k \neq -2$ / $k \neq -1$ vkj $k \neq -2$ (D) $k \neq -1$ and $k \neq 2$ / $k \neq -1$ vkj $k \neq 2$
34. Given that $\log_x y$, $\log_y x$, $\log_y z$ are in GP, $xyz = 64$ and x^3, y^3, z^3 are in AP. /fn; k x; k gsf d $\log_x y$, $\log_y x$, $\log_y z$ GP e; g; $xyz = 64$ gsf vkj x^3, y^3, z^3 e; AP gA
Which one of the following is correct? /fuEufyf [kr e; l s dku&l k l gh gA
 xy, yz and zx are / xy, yz vkj zx
- (A) in AP Only / dny AP e; g; (B) In GP only / dny GP e; g;
(C) In both AP and GP / AP vkj GP nkuka e; g; (D) Neither in AP nor in GP / u rks AP e; vkj u gh GP e; g;
35. If $y = \log_{10} x + \log_x 10 + \log_x x + \log_{10} 10$ then what is $\left(\frac{dy}{dx}\right)_{x=10}$ equal to? / ; fn $y = \log_{10} x + \log_x 10 + \log_x x + \log_{10} 10$ g; rks $\left(\frac{dy}{dx}\right)_{x=10}$ fdl ds cjkj gA
- (A) 10 (B) 2
(C) 1 (D) 0
36. A point is chosen at random inside a rectangle measuring 6 inches by 5 inches. What is the probability that the randomly selected point is at least one inch from the edge of the rectangle? / 6 bp ycs vkj 5 bp pkm; , d vk; r ds vrnj , d fcnq ; knfPNdr% pjk tkrk gA bl dh ckr; drk D; k gsf d ; knfPNdr% pps x, ml fcnq dh ml vk; r ds djk l s njh de&l &de , d bp gA
- (A) $\frac{2}{3}$ (B) $\frac{1}{3}$
(C) $\frac{1}{4}$ (D) $\frac{2}{5}$
37. What is the acute angle between the lines represented by the equations $y - \sqrt{3}x - 5 = 0$ and $\sqrt{3}y - x + 6 = 0$? / l ehdj .k; $y - \sqrt{3}x - 5 = 0$ vkj $\sqrt{3}y - x + 6 = 0$ }jk fu: fi r js[kkvk; ds chp dk U; u dks k D; k gA
- (A) 30° (B) 45°
(C) 60° (D) 75°
38. Let z_1, z_2 and z_3 be non-zero complex numbers satisfying $z^2 = i\bar{z}$, where $i = \sqrt{-1}$. /eku yift, fd z_1, z_2 vkj , z_3 शून्येतर सम्मिश्र संख्याएँ हैं, जो $z^2 = i\bar{z}$ को संतुष्ट करती हैं, जहाँ $i = \sqrt{-1}$ gA
What is $z_1 + z_2 + z_3$ equal to? / $z_1 + z_2 + z_3$ fdl ds cjkj gA
- (A) i (B) $-i$
(C) 0 (D) 1
39. Consider a parallelogram whose vertices are $A(1, 2), B(4, y), C(x, 6)$ and $D(3, 5)$ taken in order. / , d l ekvj pr[kit] जिसके शीर्ष, एक क्रम में, $A(1, 2), B(4, y), C(x, 6)$ vkj $D(3, 5)$ g; i j fopkj dlft, A
What is the value of $AC^2 - BD^2$? / $AC^2 - BD^2$ dk eku D; k gA
- (A) 25 (B) 30
(C) 36 (D) 40
40. Let $f: R \rightarrow R$ be a function such that $f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3)$ for $x \in R$. /eku yift, fd , d Qyu $f: R \rightarrow R$ bl cdkj gsf d $x \in R$ ds fy, $f(x) = x^3 + x^2 f'(1) + x f''(2) + f'''(3)$ gA
What is $f'(1)$ equal to? / $f'(1)$ fdl ds cjkj gA
- (A) -6 (B) -5
(C) 1 (D) 0
41. The mean of the series x_1, x_2, \dots, x_n is \bar{X} . If x_2 is replaced by λ , then what is the new mean? / Js kh x_1, x_2, \dots, x_n dk ek; \bar{X} g; ; fn x_2 dks λ }jk cfrLFkfi r fd; k tkrk g; rks u; k ek; ; D; k gkxk\
- (A) $\bar{X} - x_2 + \lambda$ (B) $\frac{\bar{X} - x_2 - \lambda}{n}$
(C) $\frac{\bar{X} - x_2 + \lambda}{n}$ (D) $\frac{n\bar{X} - x_2 + \lambda}{n}$

42. Let $f: R \rightarrow R$ be a function such that $f(x) = x^3 + x^2f'(1) + xf''(2) + f'''(3)$ for $x \in R$. Consider the following:
- $f(2) = f(1) - f(10)$
 - $f''(2) - 2f'(1) = 12$
- Which of the above is/are correct?
- (A) 1 Only (B) 2 Only
(C) both 1 and 2 (D) Neither 1 nor 2
43. The number 0.0011 in binary system represents
- (A) rational number $3/8$ in decimal system (B) rational number $1/8$ in decimal system
(C) rational number $3/16$ in decimal system (D) rational number $5/16$ in decimal system
44. Let α and β ($\alpha < \beta$) be the roots of the equation $x^2 + bx + c = 0$, where $b > 0$ and $c > 0$. Consider the following:
- $\alpha + \beta + \alpha\beta > 0$
 - $\alpha^2\beta + \beta^2\alpha > 0$
- Which of the above is/are correct?
- (A) 1 Only (B) 2 Only
(C) both 1 and 2 (D) Neither 1 nor 2
45. A plane P passes through the line of intersection of the planes $2x - y + 3z = 2$, $x + y - z = 1$ and the point $(1, 0, 1)$. What are direction ratios of the line of intersection of the given planes?
- (A) $(2, -5, -3)$ (B) $(1, -5, -3)$
(C) $(2, 5, 3)$ (D) $(1, 3, 5)$
46. Consider the equation $k \sin x + \cos 2x = 2k - 7$. If the equation possesses solution, then what is the minimum value of k ?
- (A) 1 (B) 2
(C) 4 (D) 6
47. For the data 3, 5, 1, 6, 5, 9, 5, 2, 8, 6 the mean, median and mode are x, y and z respectively. Which one of the following is correct?
- (A) $x = y \neq z$ (B) $x \neq y = z$
(C) $x \neq y \neq z$ (D) $x = y = z$
48. Which of the following determinants have value 'zero'?
- $\begin{vmatrix} 41 & 1 & 5 \\ 79 & 7 & 9 \\ 29 & 5 & 3 \end{vmatrix}$
 - $\begin{vmatrix} 1 & a' & b + c \\ 1 & b & c + a \\ 1 & c & a + b \end{vmatrix}$
 - $\begin{vmatrix} 0 & c & b \\ -c & 0 & a \\ -b & -a & 0 \end{vmatrix}$
- Select the correct answer using the code given below.
- (A) 1 and 2 only (B) 2 and 3 only
(C) 1 and 3 only (D) 1, 2 and 3
49. If the total number of observations is 20, $\sum x_i = 1000$ and $\sum x_i^2 = 84000$, then what is the variance of the distribution?
- (A) 1500 (B) 1600
(C) 1700 (D) 1800

50. If $\log_a(ab) = x$, then what is $\log_b(ab) = x$ equal to? / $\log_a(ab) = x$ गैर $\log_b(ab) = x$ fdl ds cjkj gj
- (A) $\frac{1}{x}$ (B) $\frac{x}{x+1}$
 (C) $\frac{x}{1-x}$ (D) $\frac{x}{x-1}$
51. Let z be a complex number satisfying $\left|\frac{z-4}{z-8}\right| = 1$ and $\left|\frac{z}{z-2}\right| = \frac{3}{2}$ / eku yhf, fd z , d l ffeJ l a; k gj tk $\left|\frac{z-4}{z-8}\right| = 1$ vkj $\left|\frac{z}{z-2}\right| = \frac{3}{2}$ को संतुष्ट करती है।
 What is $|z|$ equal to? / $|z|$ fdl ds cjkj gj
- (A) 6 (B) 12
 (C) 18 (D) 36
52. What is the number of ways in which 3 holiday travel tickets are to be given to 10 employees of an organization, if each employee is eligible for any one or more of the tickets? / d l xBu ds 10 depkj; k dks N/Vh; k=k ds 3 fVdV nus ds rjhdka dh l a; k D; k gj; fn qR; d depkjh, d; k, d l s vf/kd fVdV ds i k= g
- (A) 60 (B) 120
 (C) 500 (D) 1000
53. A card is drawn from a well-shuffled deck of 52 cards. What is the probability that it is queen of spade? / 52 तारों की एक अच्छी तरह फेंटी हुई गड्डी में से एक तारा निकाला जाता है। वह प्रायिकता क्या है कि यह हुकुम की रानी है।
- (A) $\frac{1}{12}$ (B) $\frac{1}{13}$
 (C) $\frac{1}{4}$ (D) $\frac{1}{8}$
54. What is the number of different messages that can be represented by three 0's and 1's? / vyx&vyx संदेशों की, जो rhu 0 vkj nks 1 jkjk fu: fi r fd, tk l drrs gj l a; k D; k gj
- (A) 10 (B) 9
 (C) 8 (D) 7
55. If one root of the equation $(l-m)x^2 + lx + 1 = 0$ is double the other and l is real, then what is the greatest value of m ? / fn l ehj .k $(l-m)x^2 + lx + 1 = 0$ dk, d ey n j s ey dk nks xqk gj vkj l okLrfod gj rks m dk vf/kdre eku D; k gj
- (A) $-\frac{9}{8}$ (B) $\frac{9}{8}$
 (C) $\frac{8}{9}$ (D) $\frac{8}{9}$
56. For two mutually exclusive events A and B , $P(A) = 0.2$ and $P(\bar{A} \cap \bar{B}) = 0.3$. What is $(P(A|A \cup B))$ equal to? / nks ijLij vi oftr ?kukvk A vkj B ds fy, $P(A) = 0.2$ vkj $P(\bar{A} \cap \bar{B}) = 0.3$ gA $(P(A|A \cup B))$ fdl ds cjkj gj
- (A) $\frac{1}{2}$ (B) $\frac{2}{5}$
 (C) $\frac{2}{7}$ (D) $\frac{2}{3}$
57. A certain type of missile hits the target with probability $p = 0.3$. What is the least number of missiles should be fired so that there is at least an 80% probability that the target is hit? / एक विशेष प्रकार के प्रक्षेपास्त्र की लक्ष्य भेदने की qk; drk $p = 0.3$ gA l; ure fdrus qk kL= nks tkus pkfg, fd y; dks Hknus dh qk; drk de l & de 80% gA
- (A) 5 (B) 6
 (C) 7 (D) None of the above
58. If m is the geometric mean of $\left(\frac{y}{z}\right)^{\log(yz)}$, $\left(\frac{z}{x}\right)^{\log(zx)}$ and $\left(\frac{x}{y}\right)^{\log(xy)}$ then what is the value of m ? / fn $\left(\frac{y}{z}\right)^{\log(yz)}$, $\left(\frac{z}{x}\right)^{\log(zx)}$ vkj $\left(\frac{x}{y}\right)^{\log(xy)}$ dk xq kkrj ek; m gj rks m dk eku D; k gj
- (A) 1 (B) 3
 (C) 6 (D) 9
59. A coin is tossed three times. What is the probability of getting head and tail alternately? / d fl Dds dks rhu ckj mNkyk tkrk gA fpr vkj i V ds, dkaj Øe l s vkus dh qk; drk D; k gj
- (A) $\frac{1}{8}$ (B) $\frac{1}{4}$
 (C) $\frac{1}{2}$ (D) $\frac{3}{4}$

60. Two independent events A and B have $P(A) = \frac{1}{3}$ and $P(B) = \frac{3}{4}$. What is the probability that exactly one of the two events A or B occurs? / नस लोर= ?kVukvka A vkj B ds fy, $P(A) = \frac{1}{3}$ vkj $P(B) = \frac{3}{4}$ gA og ckf; drk D; k gS fd A ; k B ea l s Bhd , d gh ?kVuk ?kVr gkxh\
- (A) $\frac{1}{4}$ (B) $\frac{5}{6}$
(C) $\frac{5}{12}$ (D) $\frac{7}{12}$

61. A random sample of 20 people is classified in the following table according to their ages: 20 ykxka ds , d ; knjfpNd परतिदर्श को उनकी आयु के अनुसार निम्नलिखित सारणी में oxhldr fd; k x; k gA

Age/ vk; q	Frequency/ ckjckjrk
15-25	2
25-35	4
35-45	6
45-55	5
55-65	3

What is the mean age of this group of people?/ ykxka ds bl l eiq dh ek/; vk; q D; k gA

- (A) 41.0 (B) 41.5
(C) 42.0 (D) 42.5
62. Three independent events, A_1 , A_2 and A_3 occur with probabilities $P(A_i) = \frac{1}{1+i}$, $i = 1, 2, 3$. What is the probability that at least one of the three events occurs?/ rhu Lora= ?kVuk, ij A_1, A_2 vkj A_3 ij f; Drk, ij $P(A_i) = \frac{1}{1+i}$, $i = 1, 2, 3$. l s ?kVr gkxh gA bl dh D; k ij kf; drk gS fd rhuks ?kVukvka ea l s de&l s de , d ?kVr gkA
- (A) $\frac{1}{4}$ (B) $\frac{2}{3}$
(C) $\frac{3}{4}$ (D) $\frac{1}{24}$

63. Let Q be the image of the point $P(-2, 1, -5)$ in the plane $3x - 2y + 2z + 1 = 0$ / eku yhf t, Q fcnq $P(-2, 1, -5)$ dk l ery $3x - 2y + 2z + 1 = 0$ ea ij frfcEc gA

Consider the following: / fuEufyf [kr ij fopkj dhft, %

- The coordinates of Q are $(4, -3, -1)$ / Q के निर्देशांक $(4, -3, -1)$ gA
- PQ is of length more than 8 units. / PQ dh yEckbz 8 bdkbz ka l s T; knk gA
- The point $(1, -1, -3)$ is the mid-Point of the line segment PQ and lies on the given plane. / fcnq $(1, -1, -3)$ js [kk [kM PQ dk e/; & fcnq gS vkj fn, x , l ery ij fLFkr gA

Which of the above statements is/are correct?/ mi ; Dr dFkuka ea l s dku l s l gh gA

- (A) 1 and 2 only (B) 2 and 3 only
(C) 1 and 3 only (D) 1, 2 and 3
64. Which one of the following differential equations represents the family of straight lines which are at unit distance from the origin?/ fuEufyf [kr vody l ehj . kka ea l s dku&l k , d mu l j y ds dy dks fu: fi r djrk gS tks ey-fcnq l s , dd njh ij gA

- (A) $(y - x \frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$ (B) $(y + x \frac{dy}{dx})^2 = 1 + (\frac{dy}{dx})^2$
(C) $(y - x \frac{dy}{dx})^2 = 1 + (\frac{dy}{dx})^2$ (D) $(y + x \frac{dy}{dx})^2 = 1 - (\frac{dy}{dx})^2$

65. A coin is tossed is three times. Consider the following events: / , d fl Dds dks rhu ckj mNkyk tkrk gA fuEufyf [kr ?kVukvka ij fopkj dhft, %

A: No head appears/ dkbz fpr (gM) ugha vkrk

B: Exactly one head appears/ ; Fkkrfk , d fpr vkrk gS

C: At least two heads appear/ de&l & de nks fpr vkrk gA

Which one of the following is correct?/ fuEufyf [kr ea l s dku&l k , d l gh gA

- (A) $(A \cup B) \cup (A \cup C) = B \cup C$ (B) $(A \cup B) \cap (A \cup C) = B \cup C$
(C) $A \cap (B \cup C) = A \cup B \cup C$ (D) $A \cap (B \cup C) = B \cap C$
66. Let $f(x) = [|x| - |x-1|]^2$. / eku yhf t, $f(x) = [|x| - |x-1|]^2$ gA
What is $f'(x)$ equal to when $x > 1$? / tc $x > 1$ gS rks $f'(x)$ fd l ds ckj gA
- (A) 0 (B) $2x-1$
(C) $4x-2$ (D) $8x-4$

67. A force $\vec{F} = 3\hat{i} + 2\hat{j} - 4\hat{k}$ is applied at the point (1, -1, 2). What is the moment of the force about the point (2, -1, 3)?
 (A) $\hat{i} + 4\hat{j} + 4\hat{k}$ (B) $2\hat{i} + \hat{j} + 2\hat{k}$
 (C) $2\hat{i} - 7\hat{j} - 2\hat{k}$ (D) $2\hat{i} + 4\hat{j} - \hat{k}$
68. In a series of 3 one-day cricket matches between teams A and B of a college, the probability of team A winning or drawing are $\frac{1}{3}$ and $\frac{1}{6}$ respectively. If a win, loss or draw gives 2, 0 and 1 point respectively, then what is the probability that team A will score 5 Points in the series?
 (A) $\frac{17}{18}$ (B) $\frac{11}{12}$
 (C) $\frac{1}{12}$ (D) $\frac{1}{18}$

69. In a study of two groups, the following results were obtained:

	Group A / I eg A	Group B / I eg B
Sample size / प्रतिदर्श आमाप	20	25
Sample mean / प्रतिदर्श माध्य	22	23
Sample standard deviation / प्रतिदर्श ekud fopyu	10	12

Which of the following statements is correct?

- (A) Group A is less variable than group B because Group A's standard deviation is smaller. / I eg A, I eg B dh vi \$kk de ifjorhZ g\$ D; kfd I eg A dk ekud fopyu y?krj g\$
 (B) Group A is less variable than Group B because Group A's sample size is smaller. / I eg A, I eg B dh vi \$kk de ifjorhZ g\$ D; kfd I eg A dk प्रतिदर्श आमाप लघुतर है।
 (C) Group A is less variable than Group B because Group A's sample mean is smaller. / I eg A, I eg B dh vi \$kk de ifjorhZ g\$ D; kfd I eg A dk प्रतिदर्श माध्य लघुतर है।
 (D) Group A is less variable than Group B because Group A's coefficient of variation is smaller. / I eg A, I eg B dh vi \$kk de ifjorhZ g\$ D; kfd I eg A dk fopj.k xq kkd y?krj g\$
70. Which of the following statements are correct?
 1. $(f \circ f)(x) = f(x)$.
 2. $(g \circ g)(x) = g(x)$ only when $x=0$. / $(g \circ g)(x) = g(x)$ dpy rHkh tc $x=0$ g\$
 3. $(g \circ (f \circ g))(x)$ can take only three values. / $(g \circ (f \circ g))(x)$ dpy rhu eku ys I drk g\$
 Select the correct answer using the code given below:

- (A) 1 and 2 only (B) 2 and 3 only
 (C) 1 and 3 only (D) 1, 2 and 3
71. Consider the following statements in respect of class intervals of grouped frequency distribution:
 1. Class intervals need not be mutually exclusive. / यह आवश्यक नहीं है fd oxl vrjky ijLij vi oftr gk\$
 2. Class intervals should be exhaustive. / वर्ग अंतराल निशेष होने चाहिए।
 3. Class intervals need not be of equal width. / यह आवश्यक नहीं है कि वर्ग अंतराल समान चौड़ाई के हों।
 Which of the above statements are correct?

- (A) 1 and 2 only (B) 2 and 3 only
 (C) 1 and 3 only (D) 1, 2 and 3
72. Three candidates solve a question. Odds in favour of the correct answer are 5:2, 4:3 and 3:4 respectively for the three candidates. What is the probability that at least two of them solve the question correctly?
 (A) $\frac{209}{343}$ (B) $\frac{134}{343}$
 (C) $\frac{149}{343}$ (D) $\frac{60}{343}$

73. What is the curve which passes through the point (1,1) and whose slope is $\frac{2y}{x}$? / फलन (1,1) | स x-अक्ष पर कौन सी वक्र है
- (A) Circle / वृत्त (B) Parabola / परवलय
(C) Ellipse / दीर्घवृत्त (D) Hyperbola / अतिपरवलय
74. A salesman has a 70% chance to sell a product to any customer. The behavior of successive customers is independent. If two customers A and B enter, what is the probability A and B enter, what is the probability that the salesman will sell the product to customer A or B? / दो क्रमिक ग्राहकों को एक ही विक्रेता को 70% संभावना है कि वह अपने उत्पाद को बेचेगा। यदि दो ग्राहक A और B क्रमशः विक्रेता के सामने आते हैं, तो विक्रेता को A या B को बेचने की संभावना क्या है?
- (A) 0.98 (B) 0.91
(C) 0.70 (D) 0.49
75. Let $f(x) = [x]$, where $[.]$ is the greatest integer function and $g(x) = \sin x$ be two real valued functions over \mathbb{R} . Which one of the following statements is correct? / $f(x) = [x]$ और $g(x) = \sin x$ दो वास्तविक मान वाले फलन हैं। निम्नलिखित में से कौन सा कथन सही है?
- (A) $\lim_{x \rightarrow 0} (f \circ g)(x)$ exists. / $\lim_{x \rightarrow 0} (f \circ g)(x)$ का अस्तित्व है। (B) $\lim_{x \rightarrow 0} (g \circ f)(x)$ exists. / $\lim_{x \rightarrow 0} (g \circ f)(x)$ का अस्तित्व है।
(C) $\lim_{x \rightarrow 0^-} (f \circ g)(x) = \lim_{x \rightarrow 0^-} (g \circ f)(x)$ (D) $\lim_{x \rightarrow 0^+} (f \circ g)(x) = \lim_{x \rightarrow 0^+} (g \circ f)(x)$
76. Two variates, x and y, are uncorrelated and have standard deviations σ_x and σ_y respectively. What is the correlation coefficient between $x+y$ and $x-y$? / दो अनसंबंधित चर x और y हैं जिनके मानक विचलन क्रमशः σ_x और σ_y हैं। $x+y$ और $x-y$ के बीच सहसंबंध गुणांक क्या है?
- (A) $\frac{\sigma_x \sigma_y}{\sigma_x^2 + \sigma_y^2}$ (B) $\frac{\sigma_x + \sigma_y}{2\sigma_x \sigma_y}$
(C) $\frac{\sigma_x^2 - \sigma_y^2}{\sigma_x^2 + \sigma_y^2}$ (D) $\frac{\sigma_x - \sigma_y}{\sigma_x \sigma_y}$
77. Consider the following statements: / निम्नलिखित कथनों पर विचार करें।
- The mean and median are equal in symmetric distribution. / सममित वितरण में माध्य और मध्यक बराबर होते हैं।
 - The range is the difference between the maximum value and minimum value in the data. / श्रेणी (MM) डेटा में अधिकतम और न्यूनतम मानों के अंतर है।
 - The sum of the areas of the rectangles in the histogram is equal to the total area bounded by the frequency polygon and the horizontal axis. / हिस्टोग्राम में आयतों के क्षेत्रों का योग आवृत्ति बहुभुज और क्षैतिज अक्ष द्वारा घेरित कुल क्षेत्रफल के बराबर होता है।
- Which of the above statements are correct? / उपरोक्त कथनों में से कौन से सही हैं?
- (A) 1 and 2 only (B) 2 and 3 only
(C) 1 and 3 only (D) 1, 2 and 3
78. What is $\int e^{\sin x} \frac{x \cos^3 x - \sin x}{\cos^2 x} dx$ equal to? / $\int e^{\sin x} \frac{x \cos^3 x - \sin x}{\cos^2 x} dx$ का मान क्या है?
- (A) $(x + \sec x) e^{\sin x} + c$ (B) $(x - \sec x) e^{\sin x} + c$
(C) $(x + \tan x) e^{\sin x} + c$ (D) $(x - \tan x) e^{\sin x} + c$
79. Let $f(x) = \begin{cases} -2, & -3 \leq x \leq 0 \\ x - 2, & 0 < x \leq 3 \end{cases}$ and $g(x) = f(|x|) + |f(x)|$. What is the value of the differential coefficient of $g(x)$ at $x = -2$? / $f(x) = \begin{cases} -2, & -3 \leq x \leq 0 \\ x - 2, & 0 < x \leq 3 \end{cases}$ और $g(x) = f(|x|) + |f(x)|$ । $g(x)$ के अवकल गुणांक का मान $x = -2$ पर क्या है?
- (A) -1 (B) 0
(C) 1 (D) 2

80. Let $f(x) = \begin{cases} -2, & -3 \leq x \leq 0 \\ x-2, & 0 < x \leq 3 \end{cases}$ and

$g(x) = f(|x|) + |f(x)|$ Eku yhf t, $f(x) = \begin{cases} -2, & -3 \leq x \leq 0 \\ x-2, & 0 < x \leq 3 \end{cases}$ vkj $g(x) = f(|x|) + |f(x)|$

Which of the following statements is/are correct?/ fuEufyf [kr dFkuka eal s dku & l k/ l s l gh gy/ga

1. $g(x)$ is differentiable at $x=0$./ $x=0$ ij $g(x)$ vodyuh; ga
2. $g(x)$ is differentiable at $x=2$./ $x=2$ ij $g(x)$ vodyuh; ga

Select the correct answer using the code given below: uhp fn, x, dM/ dk iz kx dj l gh mRrj pfu, %

- | | |
|------------------|---------------------|
| (A) 1 only | (B) 2 only |
| (C) Both 1 nor 2 | (D) neither 1 nor 2 |

81. Let the random variable X follow $B(6, p)$. If $16P(X=4) = P(X=2)$, then what is the value of p ?/ eku yhf t, fd ; knj fPpd pj $X, B(6, p)$ dk vuq j.k djr k g; ; fn $16P(X=4) = P(X=2)$, rks p dk eku D; k ga

- | | |
|-------------------|-------------------|
| (A) $\frac{1}{3}$ | (B) $\frac{1}{4}$ |
| (C) $\frac{1}{5}$ | (D) $\frac{1}{6}$ |

82. $f(x) = \begin{cases} e^x - 1, & x > 0 \\ 0, & x = 0 \end{cases}$ be a real valued function.

Eku yhf t, $f(x) = \begin{cases} e^x - 1, & x > 0 \\ 0, & x = 0 \end{cases}$, d okLrfod eku Qyu ga

Which of the following statements is/are correct?/ fuEufyf [kr dFkuka eal s dku & l k, d l gh ga

1. $f(x)$ is right continuous at $x=0$./ $x=0$ ij $f(x)$ nf{k.k l r r ga
2. $f(x)$ is discontinuous at $x=1$./ $x=1$ ij $f(x)$ vl r r ga

Select the correct answer using the code given below: uhp fn, x, dM/ dk iz kx dj l gh mRrj pfu, %

- | | |
|------------------|---------------------|
| (A) 1 only | (B) 2 only |
| (C) Both 1 nor 2 | (D) Neither 1 nor 2 |

83. A medicine is known to be 75% effective to cure a patient . If the medicine is given to 5 patients , what is the probability that at least one patient is cured by this medicine?/ dkbz nok fd l h jkxh dks jkxehDr djus ds fy, 75% dkj xj tkuh tkrh ga ; fn ; g nok 5 jkfx; ka dks nh tkrh g; rks bl dh D; k ij kf; drk g; fd bl nok l s de & l & de , d jkxh jkxehDr gks tk, \

- | | |
|-------------------------|------------------------|
| (A) $\frac{1}{1024}$ | (B) $\frac{243}{1024}$ |
| (C) $\frac{1023}{1024}$ | (D) $\frac{781}{1024}$ |

84. A line L , passes through the point $P(5,-6,7)$ and is parallel to the planes $x+y+z=1$ and $2x-y-2z=3$. , d js [kk L, fclnq $P(5,-6,7)$ l s gksdj xjtjrh g; vkj l eryka $x+y+z=1$ vkj $2x-y-2z=3$. Ds l ekarj ga

What are the direction ratios of the line of intersection of the given planes?/ fn, x, l eryka dh ij frPNn js [kk ds fnd vuq kr D; k ga

- | | |
|--------------------------------|----------------------------------|
| (A) $\langle 1, 4, 3 \rangle$ | (B) $\langle -1, -4, 3 \rangle$ |
| (C) $\langle 1, -4, 3 \rangle$ | (D) $\langle -1, -4, -3 \rangle$ |

85. What is the order of the differential equation $\frac{dx}{dy} + \int y dx = x^3$?/ vody l eh dj .k $\frac{dx}{dy} + \int y dx = x^3$ dh dkfV D; k ga

- | | |
|-------|---|
| (A) 1 | (B) 2 |
| (C) 3 | (D) Cannot be determined/ fu/kkfjr ugha dh tk l drh |

86. For 10 observations on price (x) and supply (y), the following data was obtained:/ dher (x) vkj i frl (y) ds 10 ij s k. ka eal fuEufyf [kr vkqM; i klr fd, x, %

$\sum x = 130, \sum y = 220, \sum x^2 = 2288,$

$\sum y^2 = 5506$ and $\sum xy = 3467.$

What is the line of regression of y on x ?/ X ij y kii samaashryon reखा क्या है\

- | | |
|------------------------|------------------------|
| (A) $Y = 0.91x + 8.74$ | (B) $Y = 1.02x + 8.74$ |
| (C) $Y = 1.02x - 7.02$ | (D) $Y = 0.91x - 7.02$ |

87. If $\int_0^{\pi/2} \frac{dx}{3\cos x + 5} = k \cot^{-1} 2$, then what is the value of k ?/ ; fn $\int_0^{\pi/2} \frac{dx}{3\cos x + 5} = k \cot^{-1} 2$, rks k dk eku D; k ga

- | | |
|-------------------|-------------------|
| (A) $\frac{1}{4}$ | (B) $\frac{1}{2}$ |
| (C) 1 | (D) 2 |

88. Which of the following statements are correct?

fuEufyf [kr dFkukā ēā l s dku & l s l gh gā

1. $g(x)$ is continuous at $x=0$. / $x=0$ ij $g(x)$ l r r gā
2. $g(x)$ is continuous at $x=2$. / $x=2$ ij $g(x)$ l r r gā
3. $g(x)$ is continuous at $x=-1$. / $x=-1$ ij $g(x)$ l r r gā

Select the correct answer using the code given below: uhrs fn, x, dM dk iz kx dj l gh mRrj pfu, %

- (A) 1 and 2 only (B) 2 and 3 only
(C) 1 and 3 only (D) 1, 2 and 3

89. What are the degree and order respectively of the differential equation satisfying $e^{y\sqrt{1-x^2}} + x\sqrt{1-y^2} = ce^x$, (where

$c > 0, |x| < 1, |y| < 1$)? / $e^{y\sqrt{1-x^2}} + x\sqrt{1-y^2} = ce^x$, (tgk $c > 0, |x| < 1, |y| < 1$) ko sntuṣṭ करने वाले अवकल समीकरण की घात (fMxjh) vjṣ dkrV (vkmj) कमश: क्या है\

- (A) 1,1 (B) 1,2
(C) 2,1 (D) 2,2

90. Let $f(x) = [|x| - |x-1|]^2$. / eku yhf t, $f(x) = [|x| - |x-1|]^2$ gā

What is $f'(x)$ equal to when $0 < x < 1$? / tc $0 < x < 1$ gā rks $f'(x)$ fdl ds cjkj gā

- (A) 0 (B) $2x-1$
(C) $4x-2$ (D) $8x-4$

91. $f(x) = \begin{cases} 3x^2 + 12x - 1, & -1 \leq x \leq 2 \\ 37 - x, & 2 < x \leq 3 \end{cases}$

Which of the following statements are correct? / fuEufyf [kr dFkukā ēā l s dku & l s l gh gā

1. $f(x)$ is continuous at $x=2$. / $x=2$ ij $f(x)$ l r r gā
2. $f(x)$ attains greatest value at $x=2$. / $x=2$ ij $f(x)$ vfkdre eku i klr djrk gā
3. $f(x)$ is differentiable at $x=2$. / $x=2$ ij $f(x)$ vodyuh; gā

Select the correct answer using the code given below: uhrs fn, x, dM dk iz kx dj l gh mRrj pfu, %

- (A) 1 and 2 only (B) 2 and 3 only
(C) 1 and 3 only (D) 1, 2 and 3

92. $f(x) = \begin{cases} 3x^2 + 12x - 1, & -1 \leq x \leq 2 \\ 37 - x, & 2 < x \leq 3 \end{cases}$

Which of the following statements is/are correct? / fuEufyf [kr dFkukā ēā l s dku & l s l gh gā

1. $f(x)$ is increasing in the interval $[-1, 2]$. / $f(x)$ vrjky $[-1, 2]$ ēā o/keku gā
2. $f(x)$ is decreasing in the interval $[2, 3]$. / $f(x)$ vrjky $[2, 3]$ ēā gjkl eku gā

Select the correct answer using the code given below: uhrs fn, x, dM dk iz kx dj l gh mRrj pfu, %

- (A) 1 only (B) 2 only
(C) Both 1 nor 2 (D) neither 1 nor 2

93. The expansion of $(x - y)^n, n \geq 5$ is done in the descending powers of x . If the sum of the fifth and sixth terms is zero, then $\frac{x}{y}$ is equal to / $(x - y)^n, n \geq 5$ dk i l kj x dh ?kkr ds vojkg h dā ēā fd; k x; k

है। यदि पाँचवें वा छठे पदों का योग शून्य है, तब $\frac{x}{y}$ fdl ds cjkj gā

- (A) $\frac{n-5}{6}$ (B) $\frac{n-4}{5}$
(C) $\frac{5}{n-4}$ (D) $\frac{5}{n-5}$

94. A student appears for tests I, II and III. The student is considered successful if he passes in tests I, II or I, III or all the three. The probabilities of the student passing in tests I, II and III are m, n and $1/2$ respectively. If the probability of the student to be successful is $1/2$, then which one of the following is correct? / dkbz Nk= i jh {kkvka I, II vjṣ III ēā cBrk gā ml Nk= dks l Qy ekuk tkrk g s tks i jh {kkvka I, II; k I, III; k I Hkh rhukā ēā mRrh. k l gks tkrk gā bl Nk= dh i jh {kkvka I, II vjṣ III में उत्तीर्ण होने की प्रायिकता कमश: m, n vjṣ $1/2$ gā; / n Nk= ds l Qy gkus dh ṣkr; drk $1/2$ gā rks fuEufyf [kr ēā l s dku & l s l gh gā

- (A) $m(1+n)=1$ (B) $n(1+m)=1$
(C) $m=1$ (D) $mn=1$

95. What is the domain of the function $f(x) = \frac{1}{\sqrt{|x|-x}}$? / Qyu $f(x) = \frac{1}{\sqrt{|x|-x}}$ dk i jkr (Mkxū) D; k gā

- (A) $(-\infty, 0)$ (B) $(0, \infty)$
(C) $0 < x < 1$ (D) $x > 1$

96. $f(x) = \begin{cases} e^{x-1}, & x > 0 \\ 0, & x = 0 \end{cases}$ be a real valued function.

Ekku yhf t, $f(x) = \begin{cases} e^{x-1}, & x > 0 \\ 0, & x = 0 \end{cases}$, d okLrfod eku Qyu gA

Which one of the following statements is correct? / fuEufyf [kr dFkuka eA l s dku & l k , d l gh gA

- (A) $f(x)$ is a strictly decreasing function in $(0, \infty)$. / $f(x)$ (B) $f(x)$ is a strictly increasing function in $(0, \infty)$. / $f(x)$, $(0, \infty)$ eA fuA rj g jkl eku Qyu gA $(0, \infty)$ eA fuA rj o/kku Qyu gA
- (C) $f(x)$ is neither increasing nor decreasing in $(0, \infty)$. / (D) $f(x)$ is not decreasing in $(0, \infty)$. / $f(x)$, $(0, \infty)$ eA g jkl eku ugha gA

97. A special dice with numbers 1, -1, 2, -2, 0 and 3 is thrown thrice. What is the probability that the sum of the numbers occurring on the upper face is zero? / 1, -1, 2, -2, 0 vkj 3 संख्याओं वाले एक विशेष पासे को तीन बार फेंका गया। ऊपरी Qyd पर आने वाली संख्याओं के योगफल के शून्य होने की प्रायिकता क्या है।

- (A) $1/72$ (B) $1/8$
(C) $7/72$ (D) $25/216$

98. Let $f(x) = [x]$, where $[.]$ is the greatest integer function and $g(x) = \sin x$ be two real valued functions over \mathbb{R} . / eku yhf t, $f(x) = [x]$, tgk [.] egRre i w kkd Qyu gA vkj $g(x) = \sin x$ \mathbb{R} ij nks okLrfod eku Qyu gA

Which of the following statements is correct? / fuEufyf [kr dFkuka eA l s dku & l k l gh gA

- (A) Both $f(x)$ and $g(x)$ are continuous at $x=0$. / $f(x)$ (B) $f(x)$ is continuous at $x=0$, but $g(x)$ is not continuous at $x=0$. / $f(x)$, $x=0$, ij l r r g j fdrq vkj $g(x)$ nkuka $x=0$ ij l r r gA $g(x)$ $x=0$, ij l r r ugh gA
- (C) $g(x)$ is continuous at $x=0$, but $f(x)$ is not continuous at $x=0$. / $g(x)$ $x=0$, ij l r r g j fdlr q $f(x)$, $x=0$ ij l r r ugha gA (D) Both $f(x)$ and $g(x)$ are discontinuous at $x=0$. / $f(x)$ nkuka $g(x)$ $x=0$ ij vl r r gA

99. A machine has three parts, A, B and C, whose chances of being defective are 0.02, 0.10 and 0.05 respectively. The machine stops working if any one of the parts becomes defective. What is the probability that the machine will not stop working? / एक मशीन के तीन पुर्जे A, B vkj C है, जिनके सदोष (fMQfDVo) होने की प्रायिकताएँ क्रमशः 0.02, 0.10 vkj 0.05 है। यदि इन पुर्जों में से कोई भी एक पुर्जा सदोष हो जाए, तो मशीन काम करना बंद कर देती है। इसकी क्या प्रायिकत है कि मशीन काम करना बंद नहीं करेगी।

- (A) 0.06 (B) 0.16
(C) 0.84 (D) 0.94

100. Let $f(x)$ be a function such that $f'(x) + x^3 f(x) = 0$. What is $\int_{-1}^1 f(x) dx$ equal to? / eku yhf t, $f(x)$, d , d k Qyu gA fd $f'(x) + x^3 f(x) = 0$. $\int_{-1}^1 f(x) dx$ fd l ds cjkj gA

- (A) $2f(1)$ (B) 0
(C) $2f(-1)$ (D) $4f(1)$

101. If the covariance between x and y is 30, variance of x is 25 and variance of y is 144, then what is the correlation coefficient? / x vkj y ds chp l g j l j . k 30 gA x dk i j l j . k 25 gA vkj y dk i j l j . k 144 gA rks l g l xq kkd D; k gA

- (A) 0.4 (B) 0.5
(C) 0.6 (D) 0.7

102. For two events, A and B, it is given that $P(A) = \frac{3}{5}$, $P(B) = \frac{3}{10}$ and $P(A|B) = \frac{2}{3}$. If \bar{A} and \bar{B} are the complementary events of A and B, then what is $P(\bar{A}|\bar{B})$ equal to? / A vkj B nks $P(A) = \frac{3}{5}$, $P(B) = \frac{3}{10}$ vkj $P(A|B) = \frac{2}{3}$ gA ; fn \bar{A} vkj \bar{B} , A vkj B dh i j d $P(\bar{A}|\bar{B})$ fd l ds cjkj gA

- (A) $\frac{3}{7}$ (B) $\frac{3}{4}$
(C) $\frac{1}{3}$ (D) $\frac{4}{7}$

103. What is $\int_1^3 |1 - x^4| dx$ equal to? / $\int_1^3 |1 - x^4| dx$ fd l ds cjkj gA

- (A) $-232/5$ (B) $-116/5$
(C) $116/5$ (D) $232/5$

104. Which of the following equations is /are correct? / fuEufyf [kr l ehdj . kka eA l s dku & l k / l s l gh gA

1. $f(-2) = f(5)$
2. $f'(-2) + f'(0.5) + f'(3) = 4$

Select the correct answer using the code given below: uhrs fn, x , dM dk iz ks dj l gh mRrj pfu, %

- (A) 1 only (B) 2 only
(C) Both 1 and 2 (D) neither 1 nor 2

105. Consider the following in respect of the function $f(x) = \begin{cases} 2+x & x \geq 0 \\ 2-x & x < 0 \end{cases}$

1. $\lim_{x \rightarrow 1} f(x)$ does not exist.
2. $f(x)$ is differentiable at $x=0$.
3. $f(x)$ is continuous at $x=0$.

Which of the above statements is / are correct?

Qyu $f(x) = \begin{cases} 2+x & x \geq 0 \\ 2-x & x < 0 \end{cases}$ ds l x/k ea fuEufyf [kr ij foPkkj dhft, %

1. $\lim_{x \rightarrow 1} f(x)$ dk vflrRo ugha gA
2. $f(x)$ $x=0$ l j vodyuh; gA
3. $f(x)$ $x=0$ l j l r r gA

- (A) 1 only (B) 3 only
(C) 2 and 3 only (D) 1 and 3 only

106. The scores of 15 students in an examination were recorded as 10, 5, 8, 16, 18, 20, 8, 10, 16, 20, 18, 11, 16, 14 and 12. After calculating the mean, median and mode, an error is found. One of the values is wrongly written as 16 instead of 18. Which of the following measures of central tendency will change? / fdl h ij h fkk ea 15 Nk=ka ds cklrkd 10, 5, 8, 16, 18, 20, 8, 10, 16, 20, 18, 11, 16, 14 vksj 12 vfhkfyf [kr fd, x, A ek/;] ekf/; dk vksj cgyd (ekM) dk l f j dyu dj us ds ckn, d r: fv ikbl xbA bu ekuka ea l s, d eku xyrh l s 18 ds cnys 16 fy [kk x; k gA dshjh; i j ofRr ds fuEufyf [kr eki ka ea l s dku & l k / l s cny tk, xk/ tk, xA

- (A) Mean and median / ek/; vksj ekf/; dk (B) Median and mode / ekf/; dk vksj cgyd
(C) mode only / dpy cgyd (D) Mean and mode / ek/; vksj cgyd

107. In a right-angled triangle ABC, if the hypotenuse $AB=p$, then what is $\overrightarrow{AB} \cdot \overrightarrow{AC} + \overrightarrow{BC} \cdot \overrightarrow{BA} + \overrightarrow{CA} \cdot \overrightarrow{CB}$ equal to? / d l eds k f=Hkqt ABC, ea; fn d. kl $AB=p$] rks $\overrightarrow{AB} \cdot \overrightarrow{AC} + \overrightarrow{BC} \cdot \overrightarrow{BA} + \overrightarrow{CA} \cdot \overrightarrow{CB}$ fdl ds cjkj gA

- (A) p (B) p^2
(C) $2p^2$ (D) $\frac{p^2}{2}$

108. There is 25% chance that it rains on any particular day. What is the probability that there is at least one rainy day within a period of 7 days? / किसी भी एक विशिष्ट दिन वर्षा होने का संयोग 25% gA 7 दिनों की अवधि में वर्षा का कम-से-कम, d fnu gkus dh i j kf; drk D; k gA

- (A) $1 - \left(\frac{1}{4}\right)^7$ (B) $\left(\frac{1}{4}\right)^7$
(C) $\left(\frac{3}{4}\right)^7$ (D) $1 - \left(\frac{3}{4}\right)^7$

109. Which one of the following statements is correct in respect of the function $f(x) = x^3 \sin x$? / Qyu $f(x) = x^3 \sin x$ ds l x/k ea fuEufyf [kr dFkuks ea l s dku & l k, d l gh gA

- (A) It has local maximum at $x=0$. / bl dk LFkkuh; उच्चिष्ठ $x=0$ l j gA (B) It has local minimum at $x=0$. / इसका स्थानीय निमिष्ठ $x=0$ l j gA
(C) It has neither maximum nor minimum at $x=0$. / $x=0$ पर न तो इसका उच्चिष्ठ है, न ही निमिष्ठ। (D) It has maximum value 1. / bl dk vf/kdre eku 1 gA

110. What is $\int \frac{x^4-1}{x^2\sqrt{x^4+x^2+1}} dx$ equal to? / $\int \frac{x^4-1}{x^2\sqrt{x^4+x^2+1}}$ fdl ds cjkj gA

- (A) $\sqrt{\frac{x^4+x^2+1}{x}} + c$ (B) $\sqrt{x^4+2-\frac{1}{x^2}} + c$
(C) $\sqrt{x^2+\frac{1}{x^2}+1} + c$ (D) $\sqrt{\frac{x^4-x^2+1}{x}} + c$

111. Let $f: A \rightarrow R$ where $A = R \setminus [0]$ is such that $f(x) = \frac{x+|x|}{x}$. On which one of the following sets is $f(x)$ continuous? / eku yhft, $f: A \rightarrow R$ t gka $A = R \setminus [0]$ bl i xkj gS fd $f(x) = \frac{x+|x|}{x}$ gA fuEufyf [kr l ePp; ka ea l s fdl i j $f(x)$ l r r gA

- (A) A (B) $B = \{x \in R : x \geq 0\}$
(C) $C = \{x \in R : x \leq 0\}$ (D) $D = R$

112. Consider the parabola $y = x^2 + 7x + 2$ and the straight line $y = 3x - 3$.
What is the shortest distance from the above point on the parabola to the line?
- (A) $\frac{\sqrt{10}}{2}$ (B) $\frac{\sqrt{10}}{5}$
(C) $\frac{1}{\sqrt{10}}$ (D) $\frac{\sqrt{5}}{4}$
113. Let \vec{a} , \vec{b} and \vec{c} be three vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, and $|\vec{a}| = 10$, $|\vec{b}| = 6$ and $|\vec{c}| = 14$.
What is the angle between \vec{a} and \vec{b} ?
- (A) 30° (B) 45°
(C) 60° (D) 75°
114. If $x dy = y dx + y^2 dy$, $y > 0$ and $y(1) = 1$, then what is $y(-3)$ equal to?
- (A) 3 only (B) -1 only
(C) Both -1 and 3 (D) neither -1 nor 3
115. Let \vec{a} , \vec{b} and \vec{c} be three vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, and $|\vec{a}| = 10$, $|\vec{b}| = 6$ and $|\vec{c}| = 14$.
What is $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ equal to?
- (A) -332 (B) -166
(C) 0 (D) 166
116. Let $\vec{a} = \hat{i} + \hat{j}$, $\vec{b} = 3\hat{i} + 4\hat{k}$ and $\vec{b} = \vec{c} + \vec{d}$, where \vec{c} is parallel to \vec{a} and \vec{d} is perpendicular to \vec{a} .
If $\vec{d} = x\hat{i} + y\hat{j} + z\hat{k}$, then which of the following equations is/are correct?
1. $y - x = 4$
2. $2z - 3 = 0$
- Select the correct answer using the code given below:
- (A) 1 only (B) 2 only
(C) Both 1 and 2 (D) neither 1 nor 2
117. What is the area bounded by the curves $|y| = 1 - x^2$?
- (A) $\frac{4}{3}$ square units (B) $\frac{8}{3}$ square units
(C) 4 square units (D) $\frac{16}{3}$ square units
118. Let $\vec{a} = \hat{i} + \hat{j}$, $\vec{b} = 3\hat{i} + 4\hat{k}$ and $\vec{b} = \vec{c} + \vec{d}$, where \vec{c} is parallel to \vec{a} and \vec{d} is perpendicular to \vec{a} .
What is \vec{c} equal to?
- (A) $\frac{3(\hat{i} + \hat{j})}{2}$ (B) $\frac{2(\hat{i} + \hat{j})}{3}$
(C) $\frac{(\hat{i} + \hat{j})}{2}$ (D) $\frac{(\hat{i} + \hat{j})}{3}$
119. A line L, passes through the point $P(5, -6, 7)$ and is parallel to the planes $x + y + z = 1$ and $2x - y - 2z = 3$.
What is the equation of the line L?
- (A) $\frac{x-5}{-1} = \frac{y+6}{4} = \frac{z-7}{-3}$ (B) $\frac{x+5}{-1} = \frac{y-6}{4} = \frac{z+7}{-3}$
(C) $\frac{x-5}{-1} = \frac{y+6}{-4} = \frac{z-7}{3}$ (D) $\frac{x-5}{-1} = \frac{y+6}{-4} = \frac{z-7}{-3}$
120. Let Q be the image of the point $P(-2, 1, -5)$ in the plane $3x - 2y + 2z + 1 = 0$.
Consider the following:
- The direction ratios of the line segment PQ are $\langle 3, -2, 2 \rangle$.
 - The sum of the squares of direction cosines of the line segment PQ is unity.
- Which of the above statements is/are correct?
- (A) 1 only (B) 2 only
(C) Both 1 and 2 (D) neither 1 nor 2



NDA MODAL TEST MATHEMATICS

1.	C
2.	A
3.	C
4.	C
5.	C
6.	D
7.	D
8.	D
9.	B
10.	C
11.	B
12.	D
13.	B
14.	C
15.	C
16.	C
17.	B
18.	C
19.	B
20.	D
21.	B
22.	D
23.	A
24.	C
25.	D
26.	A
27.	D
28.	D
29.	C
30.	C

31.	D
32.	A
33.	A
34.	C
35.	D
36.	D
37.	A
38.	C
39.	C
40.	B
41.	D
42.	C
43.	C
44.	B
45.	A
46.	B
47.	D
48.	D
49.	C
50.	D
51.	A
52.	D
53.	A
54.	A
55.	B
56.	B
57.	A
58.	A
59.	B
60.	D

61.	B
62.	C
63.	D
64.	C
65.	D
66.	A
67.	C
68.	D
69.	D
70.	C
71.	B
72.	A
73.	B
74.	B
75.	D
76.	C
77.	D
78.	B
79.	C
80.	D
81.	C
82.	D
83.	C
84.	C
85.	B
86.	B
87.	B
88.	D
89.	A
90.	D

91.	A
92.	C
93.	B
94.	A
95.	A
96.	B
97.	D
98.	C
99.	C
100.	C
101.	B
102.	A
103.	D
104.	A
105.	B
106.	D
107.	B
108.	D
109.	B
110.	C
111.	A
112.	C
113.	C
114.	A
115.	B
116.	D
117.	B
118.	A
119.	A
120.	C